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Published in: Journal of Hydrometeorology

DOI: 10.1175/JHM-D-12-0117.1

Publication date: 2013

Document Version Publisher's PDF, also known as Version of record

Citation for published version (APA):

Mallick, K., Jarvis, A., Tu, K., Fischer, J., Boegh, E., & Niyogi, D. (2013). Latent heat flux and canopy conductance based on Penman-Monteith and Bouchet's complementary hypothesis: validation over diverse biomes. *Journal of Hydrometeorology*, *14*(2), 419-442. https://doi.org/10.1175/JHM-D-12-0117.1

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# Latent Heat Flux and Canopy Conductance Based on Penman–Monteith, Priestley–Taylor Equation, and Bouchet's Complementary Hypothesis

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(Manuscript received 9 August 2012, in final form 2 November 2012)

#### ABSTRACT

A novel method is presented to analytically resolve the terrestrial latent heat flux ( $\lambda E$ ) and conductances (boundary layer  $g_B$  and surface  $g_S$ ) using net radiation ( $R_N$ ), ground heat flux (G), air temperature ( $T_a$ ), and relative humidity (RH). This method consists of set of equations where the two unknown internal state variables ( $g_B$  and  $g_S$ ) were expressed in terms of the known core variables, combining diffusion equations, the Penman-Monteith equation, the Priestley-Taylor equation, and Bouchet's complementary hypothesis. Estimated  $\lambda E$  is validated with the independent eddy covariance  $\lambda E$  observations over Soil Moisture Experiment 2002 (SMEX-02); the Global Energy and Water Cycle Experiment (GEWEX) Continental-Scale International Project (GCIP) selected sites from FLUXNET and tropics eddy flux, representing four climate zones (tropics, subtropics, temperate, and cold); and multiple biomes. The authors find a RMSE of 23.8-54.6 W m<sup>-2</sup> for hourly  $\lambda E$  over SMEX-02 and GCIP and 23.8–29.0 W m<sup>-2</sup> for monthly  $\lambda E$  over the FLUXNET and tropics. Observational and modeled evidence in the reduction in annual evaporation (E) pattern on the order of 33% from 1999 to 2006 was found in central Amazonia. Retrieved  $g_s$  responded to vapor pressure deficit, measured  $\lambda E$ , and gross photosynthesis in a theoretically robust behavior. However, the current scheme [Penman–Monteith–Bouchet–Lhomme (PMBL)] showed some overestimation of  $\lambda E$  in limited soil moisture regimes. PMBL provides similar results when compared with another Priestley–Taylor–based  $\lambda E$ estimation approach [Priestley-Taylor-Jet Propulsion Laboratory (PT-JPL)] but with the advantage of having the conductances analytically recovered.

#### 1. Introduction

Accurate surface energy balance is an important integral objective of the land surface model (LSM) and hydrology schemes embedded within the climate and Earth system models. Central to the surface energy balance is the latent heat flux ( $\lambda E$ ) (or evaporation E) that drives the global atmospheric circulation (Numaguti 1993; Trenberth et al. 2002), contributes significant variability (Lohmann et al. 1998; Werth and Avissar 2004) in the global hydrological cycle, and is identified as

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DOI: 10.1175/JHM-D-12-0117.1

an essential climate variable. Some recent studies have demonstrated significant disagreement among climate models, attributed mainly to the differences in the LSMs associated with them, and  $\lambda E$  has been identified as one of the important land surface process variables where major attention is needed (Pitman 2003).

To date, the methods for estimating  $\lambda E$  and its internal state variables (canopy conductance  $g_S$  and boundary layer conductance  $g_B$ ) have been largely based on unidimensional computational models having various LSMs in their core (Bonan 1995; Foley et al. 1996; Sellers et al. 1997; Niyogi and Raman 1997). While  $\lambda E$ estimates from the LSM forward runs are commonly compared with the eddy covariance (EC) data, those models are generally calibrated over some specific sites,

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and their independent global evaluation on other sites produces significant uncertainty (Bonan 2008).

The Penman-Monteith equation (PME; Penman 1948; Monteith 1965) is the most widely accepted method for estimating  $\lambda E$  from the terrestrial surfaces (Sumner and Jacobs 2005). The main advantage of the PME is that it does not require any surface temperature information. However, the disadvantage of PME is that, unlike the standard meteorological variables, the boundary layer conductance  $(g_B)$  and the canopy (or stomatal) conductance  $(g_S)$  are not available as paired observations. Therefore, PME requires information about the surface roughness and atmospheric stability-instability conditions to estimate both  $g_B$  and  $g_S$ . Measuring  $g_S$  at the leaf level and integration for the whole canopy is difficult and uncertain, while modeling  $g_S$  is error prone because plant physiological processes are controlled both by the physical environment and by the strategic behavior of plants for their optimal functioning (Katul et al. 2010). Although it would be possible to assume a mechanistic (Leuning 1995), empirical (Jarvis 1976), or semiempirical model (Ball et al. 1987) for  $g_S$ , unlike  $\lambda E$ , no universally agreed predictors for  $g_S$  have been identified. All the commonly used  $g_S$  models were originally derived from direct measurements of  $g_S$  in controlled laboratory environments. These environments do not necessarily capture spatiotemporal heterogeneity of the atmospheric and land surface states. Furthermore, these models were developed based on data collected from leaf-level measurements. For hydrological applications and LSMs, canopy-level  $g_S$  is required. The complex structure of canopies, heterogeneity of leaf physiological features, and variations within canopy microclimate make  $g_S$  significantly variable among the plant leaves. This makes it difficult to accurately derive the lumped canopy-scale  $g_S$  values from the leaf-level measurements. Upscaling of leaf-to-canopy  $g_S$  involves substantial simplifications and assumptions that could lead to large uncertainties.

Specification of  $g_B$  is equally complicated because of differences in the boundary layer conductance between the surface and the air and the boundary layer conductance between the canopy source height and the air above the canopy (Troufleau et al. 1997). This difference is empirically adjusted through introducing an "excess" conductance between the canopy source height and the surface (Troufleau et al. 1997), which, in the heterogeneous surface condition, is a complex function of canopy geometry and wind profile structure within the canopy. Estimating  $g_B$  through such an approach involves a significant amount of empiricism to specify the surface roughness lengths, displacement height, and stability–instability criteria (Thom 1975; Choudhury et al. 1986; Troufleau et al. 1997), which are not time and space invariant. While the parameterized  $g_B$  has been used with modest success, large-scale application is still highly uncertain. Given the reasons described above, an alternative, therefore, may be to analytically recover  $g_B$  and  $g_S$  from the data itself and then try to estimate  $\lambda E$ . Boegh et al. (2002) and Boegh and Soegaard (2004) had demonstrated an approach while estimating  $\lambda E$  and conductances using remote sensing data that highlights the possibilities of resolving surface energy balance nonparametrically.

In this study, we describe a method for retrieving  $g_B$ and  $g_S$  using a semi-nonparametric approach followed by the estimation of  $\lambda E$ . The method centers on combining the Penman–Monteith equation (Penman 1948; Monteith 1965), the Priestley–Taylor equation (Priestley and Taylor 1972) and Bouchet's (Bouchet 1963) complementary hypothesis in conjugation with the diffusion equations of scalar transfer. It only requires inputs of net radiation ( $R_N$ ), ground heat flux (G), air temperature ( $T_a$ ), and relative humidity (RH) or vapor pressure ( $e_a$ ). An inherent advantage is that no calibration or spinup is needed, so the method has spatiotemporal scalability (from hourly to annual and landscape to globe).

The objectives of the paper are 1) to develop a seminonparametric  $\lambda E$  estimation method based on combining the Penman–Monteith and Priestley–Taylor equations with diffusion equations and Bouchet's complementary hypothesis, 2) to assess the ability of the scheme to capture the temporal variability of  $\lambda E$  over different agricultural and forest ecosystems in different climate zones using atmospheric eddy covariance data, and 3) to evaluate the retrieved canopy conductance.

In this study, a range of radiation, meteorological and surface flux datasets from diverse climate zones covering multiple biome types are compiled and used. These include half-hourly data from international experiments [e.g., Soil Moisture Experiment 2002 (SMEX-02; Prueger et al. 2005) and the Global Energy and Water Cycle Experiment (GEWEX) Continental-Scale International Project (GCIP; National Research Council 1998)] and monthly data from FLUXNET and related eddy covariance tower sites (Baldocchi et al. 2001). While retrieving  $g_B$  and  $g_S$ , we also retrieved four additional variables: vapor pressure of the evaporating front  $(e_s)$ , saturation vapor pressure of the evaporating front  $(e_s^*)$ , evaporative fraction (EF), and aerodynamic and air temperature difference (dT). Section 2 describes the derivation of expressions for all six variables. Section 3 describes the sensitivity analysis methodology, while the description of the datasets is given in section 4. The validation of  $\lambda E$  and the analysis of the retrieved  $g_S$  is detailed in section 5. Study results are discussed in

TABLE 1. List of variable retrieved and the equations used in the study.

Unknown variables	Name	Equation	Inputs
$g_B$	Boundary layer conductance	$g_B = \frac{\Phi}{\rho C_p \left[ dT + \frac{e_S - e_a}{\gamma} \right]}$	
$g_S$	Canopy conductance	$g_S = Mg_B \frac{e_S^* - e_a}{e_S^* - e_S}$	
$e_S$	Actual vapor pressure of the evaporating front	$e_S = e_a + M(e_S^* - e_a)$	
dT	Aerodynamic and air temperature difference	$dT = \left(\frac{e_S - e_a}{\gamma}\right) \left(\frac{1 - \mathrm{EF}}{\mathrm{EF}}\right)$	$R_N, G, T_a, \text{ and } RH$
$e_S^*$	Saturation vapor pressure of the evaporating front	$e_S^* = e_a^* + \Delta dT$	
EF	Evaporative fraction	$EF = \frac{k\alpha\Delta}{2\Delta + \gamma \left(2 + \frac{g_B}{g_S}\right)}$	

section 6, and the strengths and limitations of the proposed approach are outlined in section 7.

### 2. Methodology

The proposed method seeks to analytically solve  $g_B$  and  $g_S$ . In deriving the expressions for  $g_B$  and  $g_S$ , we have also introduced four more unknown variables  $(e_S, e_S^*, \text{EF}, \text{ and } dT)$ . The core equations are given in Table 1, and their detailed derivation is explained below.

### a. Expression for $g_B$

The surface energy balance equation is written as

$$\Phi = H + \lambda E,\tag{1}$$

where  $\Phi$  is net available energy ( $\cong R_N - G$ ), *H* is sensible heat flux,  $\lambda E$  is latent heat flux,  $R_N$  is net radiation, and *G* is conductive surface heat flux or ground heat flux. All the fluxes are in watts per meter squared:

$$H = \rho C_P g_B dT, \qquad (2)$$

$$\lambda E = \frac{\rho C_P}{\gamma} g_B(e_S - e_a), \qquad (3)$$

where  $\rho$  is air density (kg m<sup>-3</sup>),  $C_P$  is specific heat of dry air (MJ kg<sup>-1</sup> K<sup>-1</sup>),  $\gamma$  is the psychrometric constant (hPa K<sup>-1</sup>), dT is the difference between the aerodynamic temperature ( $T_{aero}$ , temperature at canopy source height) and air temperature  $T_a$  (K), and  $e_S$  is the actual vapor pressure (hPa) of the evaporating front where  $T_{aero}$  is satisfied.  $T_{aero}$  is the temperature of the thin boundary layer in the immediate vicinity of the surface level and is responsible for the transfer of heat from the surface to the atmosphere. Generally, dT is expressed as the difference between the radiometric surface temperature ( $T_{sfc}$ ) and the air temperature ( $T_a$ ), but  $T_{\rm sfc}$  is not the true temperature that is responsible for transferring the sensible heat flux (Troufleau et al. 1997). In spite of the apparent simplicity of Eq. (2), the main limitation lies in the definition of surface temperature. Considering the vertical extension of vegetation or canopy, the concept of "surface" and its associated level is quite confusing (Norman and Campbell 1998). Equation (2) is specially inferred from the aerodynamic transfer equations, which means that  $T_{\rm sfc}$  is theoretically an air temperature at the surface, which is different from the physical temperature of the surface (Monteith 1965). The level that satisfies  $T_{aero}$  is defined as the source height where wind speed is zero and  $T_{aero}$  is obtained by extrapolating the logarithmic profile of  $T_a$  down to that level. Stewart and Thom (1973) postulated that the effective source of sensible heat flux is located at a lower level that the effective sink of momentum. Hence, dT is equivalent to the difference between  $T_{aero}$  and  $T_a$  and is treated as an unknown state variable in the present study. By combining Eqs. (1), (2), and (3) and expressing for  $g_B$ , we get

$$g_B = \frac{\Phi}{\rho C_P \left[ dT + \frac{(e_S - e_a)}{\gamma} \right]}.$$
 (4)

#### b. Expression for $g_S$

An equation of canopy (or stomatal) conductance  $(g_S)$  is obtained from the following diffusion equation expression. According to the diffusion equation,  $\lambda E$  can be also expressed as

$$\lambda E = \frac{\rho C_P}{\gamma} g_S(e_S^* - e_S) \tag{5}$$

and

$$\lambda E = M \times PE = M \frac{\rho C_P}{\gamma} g_B(e_S^* - e_a), \qquad (6)$$



FIG. 1. Temporal patterns of  $M (= RH^{VPD})$  ( $f_{SM}$  in Fisher et al. 2008) and relative surface moisture ( $R_M$ ) along with the  $R_N$  and  $\lambda E$  over the (a)–(d) four prime climates (according to Köppen's classification) of the world. These are the observational data from the FLUXNET eddy covariance network, where representative sites falling under the individual climate regions are exemplified. This clearly shows the strong control of moisture on  $\lambda E$  in the dry climate and little control of moisture in the temperate and cold climate. These figures also reveal the control of radiation on  $\lambda E$  in the temperate and cold climate, whereas in the tropical and subtropical dry climate both moisture and radiation impose strong controls on  $\lambda E$ .

where  $e_s^*$  is saturation vapor pressure (hPa) of the evaporating front and M is the limiting factor that is responsible for constraining potential evaporation (PE) into  $\lambda E$ . Equation (6) resembles the  $\alpha$ - $\beta$  formulations of  $\lambda E$  (Noilhan and Planton 1989; Lee and Pielke 1992; Cahill et al. 1999). From Eqs. (5) and (6), we can express  $g_s$  in terms of  $g_B$ ,  $e_s^*$ ,  $e_s$ ,  $e_a^*$ ,  $e_a$ , and M:

$$g_{S} = M \times g_{B} \frac{e_{S}^{*} - e_{a}}{e_{S}^{*} - e_{S}}.$$
 (7)

For the vegetation, water vapor transfer occurs from within the vegetation (transpiration) and from the immediate vicinity of the vegetation surface (evaporation). For dense canopies and moist soils,  $T_{\rm sfc}$  may approach the true aerodynamic temperature of the evaporating surface (Lhomme et al. 2000). The stomatal cavities can be assumed to be saturated; therefore,  $e_S^*$  of dense canopies can always be estimated from  $T_{\rm sfc}$ . But for extremely dry, bare soil, the evaporating front is located much below the dry surface layer of different thermal property, and the true  $T_{\rm sfc}$  may be different than the surface  $T_{\rm sfc}$  by a few degrees. Despite the availability of  $T_{\rm sfc}$  data from the current generation of polar orbiting satellites,  $T_{\rm sfc}$  is not used in the present study because of the differences between the physical versus aerodynamic temperature, as described above. Therefore,  $e_s^*$  was treated as an unknown variable and expressed according to Monteith (1965) [Eq. (14) and Table 1].

We hypothesize M to be a stress factor that arises because of moisture or wetness availability (or unavailability). A wide range of M can be found in the natural ecosystems in different climatic regions of the world. The tropical region has little variability in M, whereas the dry climate (covering the Mediterranean savanna and arid-semiarid region) has an extremely large variability in M (Fig. 1). Series of research have already expressed M as a function of soil moisture, soil water potential, and atmospheric vapor pressure deficit (VPD; Noilhan and Planton 1989; Kondo et al. 1990).

Fisher et al. (2008) expressed  $M = RH^{VPD}$  (RH in a fraction and VPD in kilopascals; equivalent to  $f_{SM}$  in Fisher et al. 2008) and found that this is equivalent to the relative extractable surface moisture  $(R_M)$ . The hypothesis was that the surface soil moisture (and, hence, extractable near-surface soil moisture) could be inferred from the atmospheric moisture and that there is no resistance to transfer between them that will ultimately prevent them from reaching equilibrium. Atmospheric resistance only delays the process of equilibration but does not prevent it, if given enough time. In contrast, plants can actively maintain disequilibrium from the atmosphere via stomatal closure. Under the conditions when M = 0 and the surface soil moisture is 0, the plants may access groundwater via deep roots that extend below the surface soil layers. This would be consistent with the occurrence of transpiration in very dry environments where  $RH \rightarrow 0$  but there is still sparse green vegetation. Therefore, the difference between  $e_s$  and  $e_a$  is very small when  $RH \rightarrow 0$ . Such conditions exist in the dry climate (arid-semiarid, savanna, temperate, and cold) where atmospheric moisture demand remains high and the vertical column from surface to subsurface is also extremely dry. On the contrary, under the influence of high RH and low atmospheric water demand (tropics, wet temperate, and wet cold climate), M tends to be high and does not impose any strong constraint on  $g_S$  and  $\lambda E$ . Vegetation transpires at the optimum rate mainly under the influence of available energy under such conditions. The characteristic pattern of M across different climates is shown in Figs. 1a-d and is calculated following the Fisher et al. (2008) equation.

The soil moisture data from active–passive microwave sensors (e.g., QuikSCAT, AMSR-E, and SMOS) can be used, but the soil moisture estimates from these current microwave satellite sensors are prone to large uncertainties, especially in the densely vegetated landscapes (Mallick et al. 2009).

In Eqs. (4) and (7), there are five unknowns:  $g_B$ ,  $g_S$ , dT,  $e_S^*$ , and  $e_S$ . We need to identify other equations to solve for the other three unknowns ( $e_S$ , dT, and  $e_S^*$ ).

### c. Expression for $e_S$

While rewriting the Penman–Monteith equation, the vapor pressure deficit at the evaporating front was given by Jarvis and McNaughton (1986) as follows:

$$e_{S}^{*} - e_{S} = \Omega(e_{S}^{*} - e_{S})_{eq} + (1 - \Omega) \text{VPD},$$
 (8)

where  $\Omega = (\Delta/\gamma + 1)/(\Delta/\gamma + 1 + g_B/g_S)$  is the decoupling coefficient, which quantifies the degree of coupling between the surface and the overlying atmosphere;  $(e_S^* - e_S)_{eq}$  is the equilibrium surface vapor pressure deficit (hPa); and  $\Delta$  is the slope of the saturation vapor pressure versus air temperature (hPa  $K^{-1}$ ). Under efficient vertical mixing of the air,  $g_B$  increases and  $\Omega \rightarrow 0$ , which implies a good surface-atmosphere coupling. According to Eq. (8), when the surface is fully coupled to the atmosphere ( $\Omega = 0$ ), the VPD is imposed at the surface. On the contrary, when the surface is completely decoupled from the atmosphere ( $\Omega = 1$ ), the surface vapor pressure deficit in that condition can be solved as  $(e_S^* - e_S)_{eq} = (\lambda E_{eq}/g_S)(\gamma/\rho C_P)$ , where  $\lambda E_{eq}$  is the equilibrium latent heat flux given as  $\lambda E_{eq} = \Phi(\Delta/\Delta + \gamma)$ (Jarvis and McNaughton 1986). When the surface-air temperature difference increases above 10°C, the linear approximation of  $\Delta$  in the Penman–Monteith equation becomes invalid (Paw U and Gao 1988). Dry bare soil very often attains this temperature difference in many parts of the world during summer. Under the decoupled condition, using nonlinear solutions for the saturated vapor pressure results the limit of  $\lambda E$  to approach the net available energy ( $\Phi$ ), which may be very different from the  $\lambda E_{eq}$  used to calculate  $(e_S^* - e_S)_{eq}$  (Paw U and Gao 1988). Therefore, the application of Eq. (8) for evaluation of  $e_s$  may produce a significant error when  $g_B/g_S$ approaches a big value (i.e., when  $g_B/g_S \rightarrow \infty$ ).

For the prediction of  $e_s$ , the decoupling coefficient  $(\Omega)$  was used to quantify the degree of coupling between the surface and the atmosphere (Jarvis and McNaughton 1986). When the surface and the atmosphere are tightly coupled  $(\Omega \rightarrow 0)$ ,  $e_s$  approaches  $e_a$ , and when the surface is fully decoupled from the atmosphere  $(\Omega \rightarrow 1)$ , water vapor starts accumulating at the surface and  $e_s$  approaches  $e_s^*$ . The limit of  $e_s$  during decoupled conditions may be calculated from the  $T_{\rm sfc}$  measurement. Earlier, Boegh et al. (2002) and Boegh and Soegaard (2004) investigated the feasibility of using  $\Omega$  as an empirical weighting factor to place  $e_s$  between its limit values,  $e_s^*$  and  $e_a$ , by using the following two equations:

$$e_{S} = \Omega h_{S_{\text{max}}} e_{S}^{*} + (1 - \Omega)e_{a}, \qquad (9a)$$

$$e_S = \Omega \Lambda e_S^* + (1 - \Omega) e_a, \qquad (9b)$$

where  $h_{S_{\text{max}}}$  is the maximum upper level for the relative air humidity at the surface, which was parameterized empirically with fractional vegetation cover and  $\Lambda$  is an adjustment factor (humidity related) analytically related to the vapor pressure and conductances. A constant value of  $\Lambda$  (=0.9) was assigned to compute evapotranspiration for a wide range of surface conditions. Looking at the description of both  $h_{S_{\text{max}}}$  and  $\Lambda$ , the surface humidity is not necessarily dependent on fractional vegetation cover, but it is dependent on surface moisture availability (M) or surface humidity (Lee and Pielke 1992). Similarly, using  $\Lambda$  as a static value may lead to errors under very dry surface conditions. Instead of using a land cover-dependent moisture variable or a constant moisture variable, we expressed the surface humidity or surface moisture availability according to Fisher et al. (2008), and  $e_s$  is expressed as follows:

$$e_{S} = e_{a} + M(e_{S}^{*} - e_{a}).$$
(10)

This equation is very similar to the expressions used by Nappo (1975), Ye and Pielke (1993), and Wetzel et al. (1984).

#### *d.* Expression for dT and $e_s^*$

After finding an expression of  $e_S$ , the next step is to find an expression of dT. Here we used the Bowen ratio ( $\beta$ ) equation (Bowen 1926):

$$\beta = \gamma \frac{dT}{e_s - e_a}.\tag{11}$$

With the assumption of surface energy balance closure,  $\beta$  can also be expressed in terms of EF as (Shuttleworth et al. 1989)

$$\beta = \frac{1 - \mathrm{EF}}{\mathrm{EF}}.$$
 (12)

The quantity EF is defined as the fraction of available energy ( $\Phi$ ) partitioned toward  $\lambda E$ . Substituting  $\beta$  in Eq. (11), we can get an expression of dT in terms of EF:

$$dT = \left(\frac{e_{S} - e_{a}}{\gamma}\right) \left(\frac{1 - \text{EF}}{\text{EF}}\right).$$
(13)

We have expressed  $e_s^*$  according to Monteith (1965):

$$e_S^* = e_a^* + \Delta dT. \tag{14}$$

While finding the expression of dT, we have introduced one extra variable, EF. Therefore, to close the system of equations, we need one more equation. The derivation of the expression for EF is described below.

### e. Expression for EF

According to the PME (Penman 1948; Monteith 1965),

$$PE_{PM} = \frac{\Delta \Phi + \rho C_P g_B VPD}{\Delta + \gamma}, \quad (15)$$

$$\lambda E = \frac{\Delta \Phi + \rho C_P g_B \text{VPD}}{\Delta + \gamma \left(1 + \frac{g_B}{g_S}\right)},\tag{16}$$

where  $\Delta$  is the slope of the saturation vapor pressure versus air temperature relationship (hPa K<sup>-1</sup>),  $\Phi$  is the net available energy driving latent heat (W m<sup>-2</sup>),  $\rho$  is air density (kg m<sup>-3</sup>),  $C_P$  is the specific heat of dry air (MJ kg<sup>-1</sup> K<sup>-1</sup>), VPD is the atmospheric vapor pressure deficit (hPa),  $\gamma$  is the psychometric constant (hPa K<sup>-1</sup>), and PE<sub>PM</sub> is the potential evaporation according to Penman. It is defined as the evaporation that would take place from a moist surface under prevailing weather conditions, limited only by the net available energy. Other terms in the above two equations are explained earlier.

Dividing Eq. (16) by Eq. (15), we get

$$\frac{\lambda E}{\text{PE}_{\text{PM}}} = \frac{\Delta + \gamma}{\Delta + \gamma \left(1 + \frac{g_B}{g_S}\right)}.$$
(17)

On regional scales, PE and  $\lambda E$  are dependent on each other. Bouchet (1963) first proposed, for a large homogeneous area with minimum advection of heat and moisture, that PE and  $\lambda E$  are strongly coupled through a complementary land-atmosphere feedback mechanism. He hypothesized that, under the conditions of constant energy supply to any given surface-atmosphere system, when the water availability becomes limited,  $\lambda E$ falls below PE, and some amount of energy becomes available. This extra energy increases the temperature and humidity gradient of the overlying air (in the form of sensible heat or longwave back radiation) and leads to an increase in PE whose magnitude is equal to the decrease in  $\lambda E$ . If moisture availability is increased,  $\lambda E$ again starts increasing and PE decreases. Under the condition of unlimited moisture supply,  $\lambda E$  equals PE is referred to as wet environment evaporation  $(ET_W)$ . If the energy budget remains unchanged and all the excess energy is converted into the sensible heat flux, a complementary relationship of the form  $\lambda E + PE = k \times ET_W$ exists, where k = 2.

According to the complementary relationship advection aridity hypothesis of Brutsaert and Stricker (1979),  $ET_W$  was approximated as the potential evaporation according to Priestley and Taylor (1972) (PE<sub>PT</sub>) and PE was expressed as the potential evaporation according to Penman (1948) (PE<sub>PM</sub>). Therefore,

$$\lambda E + PE_{PM} = k \times ET_{PT}.$$
 (18)

From the above expression,  $ET_W$  is a constant for a prevailing atmospheric condition and moisture availability. According to traditional Budyko approach (Budyko et al. 1962; Roderick and Farquhar 2004), in case of complementarity, the regional  $\lambda E$  is limited by moisture availability in the arid climate and  $\lambda E$  is limited by energy availability in the humid climate. However, the complementary relationship allows regional PE to depend on regional  $\lambda E$  in a complementary manner throughout any range of moisture and energy availability (Ramirez et al. 2005).

Some theoretical arguments suggest that the hypothesis of 1:1 compensation between  $\lambda E$  and PE around ET<sub>W</sub> is only partially fulfilled (Lhomme 1997; Sugita et al. 2001). Lhomme (1997) have shown that k is a function of both  $g_S$  and  $g_B$ , and k is equal to 2 when  $g_S = 0$  (i.e., under the wettest surface condition) or when  $g_B \to \infty$  (i.e., k tends to be 2 as the surface appears smooth). Otherwise, the expression of k becomes  $k = [2 + 1/(1 + \varepsilon)(g_B/g_S)]/\alpha$ . However, very recently Ramirez et al. (2005) found observational evidence of the complementary relationship and confirmed the value of k to be 2 (standard deviation  $\pm 0.02$ ). Therefore, we opted for k = 2 in the present study;  $\alpha$  is the Priestley–Taylor coefficient (1.26) and  $\varepsilon = \Delta/(\Delta + \gamma)$ . From the above equation,

$$PE_{PM} = k \times PE_{PT} - \lambda E.$$
(19)

Dividing both sides of Eq. (19) by  $\lambda E$ , we get

$$\frac{\lambda E}{\mathrm{PE}_{\mathrm{PM}}} = \frac{\lambda E}{k \times \mathrm{PE}_{\mathrm{PT}} - \lambda E}.$$
(20)

Dividing the numerator and denominator of the righthand side of Eq. (19) by PE<sub>PT</sub>, we get

$$\frac{\lambda E}{\mathrm{PE}_{\mathrm{PM}}} = \frac{\frac{\lambda E}{\mathrm{PE}_{\mathrm{PT}}}}{k - \frac{\lambda E}{\mathrm{PE}_{\mathrm{PT}}}}.$$
(21)

According to Priestley and Taylor (1972),

$$PE_{PT} = \alpha \frac{\Delta}{\Delta + \gamma} \Phi,$$

where  $\Phi$  can also be expressed as  $\Phi = (\lambda E/EF)$ . Therefore,

$$PE_{PT} = \alpha \frac{\Delta}{\Delta + \gamma} \frac{\lambda E}{EF}$$
$$\frac{\lambda E}{PE_{PT}} = \frac{\Delta + \gamma}{\alpha \Delta} EF.$$
 (22)

Now, substituting this expression of  $\lambda E/PE_{PT}$  from (22) into (21) and after some algebra,

$$\frac{\lambda E}{\text{PE}_{\text{PM}}} = \frac{\text{EF}(\Delta + \gamma)}{k\alpha\Delta - \text{EF}(\Delta + \gamma)}.$$
(23)

Replacing  $\lambda E/PE_{PM}$  between (17) and (23), we can express EF in terms of conductance:

$$\frac{\mathrm{EF}(\Delta+\gamma)}{k\alpha\Delta-\mathrm{EF}(\Delta+\gamma)} = \frac{\Delta+\gamma}{\Delta+\gamma\left(1+\frac{g_B}{g_S}\right)}$$

After some algebra, the final expression of EF in terms of  $g_B$  and  $g_S$  is

$$EF = \frac{k\alpha\Delta}{2\Delta + \gamma \left(2 + \frac{g_B}{g_S}\right)}.$$
 (24)

Now we can solve Eqs. (4), (7), (10), (13), (14), and (24) to retrieve  $g_B$ ,  $g_S$ , dT,  $e_S$ ,  $e_S^*$ , and EF. We name our method Penman–Monteith–Bouchet–Lhomme (PMBL).

### 3. Sensitivity analysis

Given that the  $\lambda E$  outputs from PMBL are dependent on the four core variables, a one-dimensional sensitivity analysis (Sanchez et al. 2009) was carried out to assess the impacts of the propagation of uncertainty of the input variables into the  $\lambda E$  estimates. The input variables ( $T_a$ , RH,  $R_N$ , and G) were changed by  $\pm 10\%$  from their reference value range, except for air temperature ( $T_a$ ), for which  $\pm 2$ -K perturbation was assigned. The method computes the relative sensitivity S of  $\lambda E$  to p uncertainties in the individual four variables. The sensitivity is finally expressed as

$$S = \frac{\lambda E_{p+} - \lambda E_{p-}}{\lambda E_r},$$

where  $\lambda E_r$  is the estimated value of  $\lambda E$  when the value of any of the four variables are at their reference value,  $\lambda E_{p+}$  is the estimated value of  $\lambda E$  when the value of any of the four variables is increased by p from its reference value without perturbing the other input variables, and  $\lambda E_{p-}$  is the estimated value of  $\lambda E$  when the value of any of the four variables is decreased by p from its reference value without perturbing the other input variables.

### 4. Datasets

According to the equations described in Table 1, estimation of  $\lambda E$  in PMBL requires information  $R_N$ , G,  $T_a$ , RH, or  $e_a$ . All four variables are available from different international flux measurement experiments, the FLUXNET network, and a tropical forest flux site database compiled by Fisher et al. (2009). An eddy covariance method was used in all cases to quantify the vertical fluxes between the ecosystem and the atmosphere from the covariance between vertical wind velocity and scalar fluctuations (Baldocchi et al. 2001). The surface energy balance was closed according to Barr et al. (2006). An energy closure fraction was estimated as  $F = (\lambda E + H)/(R_N - G)$  by linear regression, forced through the origin, with  $R_N$  and G as the independent variables and

Experiment-data source	Years	Spatial resolution	Temporal resolution	Biome type	Reference
SMEX-02	2002	Eddy covariance footprint	30 min	Agroecosystems	Prueger et al. (2005)
GCIP	1996–1998	Eddy covariance footprint	30 min	Agroecosystems	National Research Council (1998)
Tropics	Varying between 1999 and 2006	Eddy covariance footprint	Monthly	Rainforest	Fisher et al. (2009)
FLUXNET	Varying between 2002 and 2006	Eddy covariance footprint	Monthly	Diverse biome from forest, grassland, agroecosystem, wetland, and savanna	Baldocchi et al. (2001)

TABLE 2. Datasets used in the evapotranspiration estimation and validation through PMBL.

 $H + \lambda E$  as dependent variables. This regression approach provided a stable and robust estimate of *F* across the entire range of  $R_N - G$ . We could also evaluate the PMBL  $\lambda E$  across all the sites because an independent measurement of  $\lambda E$  was available. Detailed descriptions of the different datasets (Table 2) are given below, and the distribution of sites is shown in Fig. 2.

### a. Data from SMACEX SMEX-02

The Soil Moisture–Atmosphere Coupling Experiment (SMACEX) (Prueger et al. 2005; Kustas et al. 2005) was conducted in conjunction with SMEX-02 during June–July 2002 in and around the Walnut Creek watershed (WCW) near Ames, Iowa. The landscape was an agroecosystem with an intensive corn and soybean production region that consisted of a network of 12 eddy covariance meteorological and flux (METFLUX) towers (6 soybean and 6 corn) (Table 3). Multiple flight tracks were also flown by a Canadian Twin Otter aircraft for evaluating the spatial variability in surface fluxes across the study area. Surface fluxes (H,  $\lambda E$ , and G),  $R_N$ ,  $T_a$ , and RH were available at half-hourly intervals through the towers. At all the sites, tower heights were maintained at approximately 2h (where h is canopy height in meters) above the surface. All of the raw data were stored during the intensive observation period for consecutive 18 days from day of year (DOY) 171 to 189.

### b. Data from the GCIP

The National Oceanic and Atmospheric Administration (NOAA)/Atmospheric Turbulence and Diffusion Division (ATDD) started operation of a long-term flux monitoring site near Bondville, Illinois, in 1996. This falls under the GCIP Enhanced Observing Period (EOP)



FIG. 2. Distribution of eddy covariance sites used in the present analysis over the prime climate zones of the world.

TABLE 3. Error statistics of the PMBL-derived $\lambda E$ over the eddy covariance sites of SMEX-02 and GCIP for both hou	urly
and daily estimates.	

						Hourly			Daily	
Experiment	Latitude (°)	Longitude (°)	Tower site ID	Crop	RMSE (W m <sup>-2</sup> )	MB (W m <sup>-2</sup> )	r	RMSE (W m <sup>-2</sup> )	MB (W m <sup>-2</sup> )	r
SMEX-02	41.983	-93.754	WC03	Soybean	37.0	-4.9	0.93	18.9	-7.2	0.75
	41.932	-93.753	WC06	Corn	43.6	-10.0	0.94	22.0	-19.7	0.89
	41.952	-93.687	WC13	Soybean	48.1	23.7	0.89	40.8	33.6	0.52
	41.945	-93.696	WC14	Soybean	53.0	-0.8	0.90	21.2	-2.5	0.75
	41.992	-93.535	WC23	Soybean	38.0	1.2	0.89	18.5	9.6	0.91
	41.992	-93.528	WC24	Corn	56.5	-21.4	0.90	13.0	1.8	0.88
	41.942	-93.539	WC25	Soybean	50.9	8.63	0.92	15.9	6.7	0.96
	41.975	-93.644	WC33	Corn	48.6	-3.7	0.90	24.6	21.8	0.97
	41.937	-93.663	WC151	Corn	41.5	-1.7	0.96	15.0	10.1	0.84
	41.937	-93.664	WC152	Corn	38.3	-5.9	0.95	10.6	-5.6	0.91
	41.934	-93.662	WC161	Soybean	35.6	-7.8	0.92	31.1	17.3	0.24
	41.935	-93.664	WC162	Soybean	40.3	-6.6	0.91	19.1	3.1	0.68
			Pooled	_	44.9	-2.0	0.90	20.9	5.8	0.78
			SMACEX aircraft	Corn–soybean mix	38.5	-0.4	0.90	—	—	—
			All corn		46.2	-5.1	0.92			_
			All soybean		44.6	10.9	0.90			_
GCIP	40.000	-88.280	Bondville	Corn	41.6	8.6	0.90			
			Bondville	Soybean	34.6	-3.3	0.94			_
			Bondville	Corn	41.6	3.4	0.91	_	_	_

program that took place in the Mississippi River basin during 1995–2000. The field consisted alternately of soybeans and corn from 1996 to 1999. Half-hourly observations of surface fluxes ( $H, \lambda E$ , and G) along with radiation and meteorological variables (e.g.,  $R_N$ ,  $T_a$ , and RH), were available at this site. The entire dataset and its detailed description are available through http://data. eol.ucar.edu/codiac. In the present study, we used data for three consecutive years from 1997 to 1999.

### c. Data from the tropical forest

The study sites (21 sites) included a wide range of tropical biome types spreading around South America, Southeast Asia, Africa, and Oceania (Table 4). Micrometeorological instruments were attached to towers extending above the tall forest canopies. Energy balance closure at the tropical forest sites in this analysis was 80% for monthly daytime averages (Fisher et al. 2009). Monthly average of  $\lambda E$ , H,  $R_N$ , G,  $T_a$ , and RH data was used based on averaging of half-hour to daily to monthly values.

### d. Data from FLUXNET

These data cover a broad spectrum of biomes, climate, and plant functional types from 15 eddy covariance sites. The sites covered five subnetworks of FLUXNET (Baldocchi et al. 2001): AmeriFlux, Asia-Flux, EuroFlux, Fluxnet Canada, and OzFlux. Here also independent measurement of  $\lambda E$  was available, along with measurements of H,  $R_N$ , G,  $T_a$ , and RH. A comprehensive description of this dataset can be found in Fisher et al. (2008).

### e. PT-JPL model

The specific reason of selecting the tropics and FLUXNET sites was to compare the PMBL results with another model [Priestley-Taylor-Jet Propulsion Laboratory (PT-JPL)] (Fisher et al. 2008, 2009) output that was based on constraining the Priestley-Taylor parameter ( $\alpha$ ) over a wide range of hydroclimatic regimes. PT-JPL is a global model for estimating  $\lambda E$ that is based on the Priestley and Taylor (1972) PE framework, where different biophysical and meteorological scalars were used to constrain PE into  $\lambda E$ . PT-JPL runs with five inputs:  $R_N$ , two vegetation indices,  $T_a$ , and  $e_a$ , to generate spatially explicit and temporally consistent  $\lambda E$  estimates. Given that the results from Fisher et al. (2008, 2009) were monthly, PMBL was also executed on the monthly scale over the tropics and FLUXNET.

### 5. Results

### a. Validation of latent heat flux

### 1) SMEX-02-SMACEX AND GCIP

PMBL was run at a temporal resolution of 30 min over the 19 days of the intensive observation period at each of the 12 flux tower sites of SMEX-02. The overall

					$\lambda E_{\rm PMBL}$		į	$\lambda E_{\rm PT-JPL}$	
Tropics EC subnetwork	Site	Latitude (°)	Longitude (°)	RMSE (W m <sup>-2</sup> )	$\frac{MB}{(W m^{-2})}$	r	RMSE (W m <sup>-2</sup> )	$\frac{MB}{(W m^{-2})}$	r
Africa	Kissoko (KIS)	-4.791	11.982	19.0	14.7	0.96	35.6	32.4	0.96
South America	Bannanal Island (BAN)	-9.824	-50.159	28.6	-11.5	0.78	23.2	17.9	0.89
	Caxiuana (CAX)	-1.719	-51.458	18.8	8.2	0.97	36.1	33.9	0.98
	Fazenda Noza Senhora (FNS)	-10.761	-62.357	16.1	15.0	0.97	28.1	27.5	0.97
	Guyaflux (GUY)	5.277	-52.928	17.3	-5.5	0.62	19.5	13.2	0.76
	La Selva (LAS)	10.423	-83.978	52.1	-45.5	0.96	31.1	-22.5	0.97
	Manaus C14 (M14)	-2.589	-60.115	8.8	3.0	0.97	12.8	9.9	0.97
	Manaus KM34 (M34)	-2.609	-60.209	5.1	-1.7	0.97	11.1	10.1	0.97
	Reserva Jaru (RJA)	-10.083	-61.931	9.4	-6.0	0.90	13.3	11.2	0.91
	Reserva Pé-de-Gigante (RPG)	-21.619	-47.649	23.8	0.3	0.91	29.7	21.2	0.92
	Santarem KM67 (KM67)	-2.856	-54.958	8.0	-4.9	0.95	17.0	15.3	0.93
	Santarem KM77 (KM77)	-3.011	-54.536	45.9	27.5	0.68	63.0	55.4	0.80
	Santarem KM83 (KM83)	-3.018	-54.971	18.9	-17.7	0.95	6.7	0.7	0.95
Oceania	Cocoflux (COC)	-15.435	167.185	12.4	-4.8	0.88	17.9	12.3	0.88
Southeast Asia	Bukit Soeharto (BKS)	0.868	117.052	22.6	14.9	0.79	29.7	22.5	0.79
	Kog-Ma (KOG)	18.800	98.900	20.1	-3.6	0.31	15.6	5.2	0.64
	Lamber Hills (LAM)	4.200	114.033	10.2	6.8	0.98	24.4	12.1	0.98
	Mae Klong (MKL)	14.582	98.850	6.6	-4.5	0.81	5.9	1.6	0.73
	Palangkaraya (PKA)	-1.655	114.036	14.9	-11.4	0.92	13.8	10.2	0.92
	Sakaerat (SKR)	14.485	101.926	25.1	5.7	0.86	32.0	21.2	0.87
	Tak (TAK)	16.622	99.433	13.6	3.2	0.78	12.5	6.8	0.87
Pooled	_	_	_	23.8	-0.4	0.92	28.4	17.1	0.93
Annual (mm)		_	_	103	2	0.95	111	157	0.94

TABLE 4. Intercomparison of PMBL $\lambda E$  statistics against  $\lambda E$  observations and PT-JPL $\lambda E$  model for individual eddy covariance sites of the tropical forest eddy covariance subnetwork.

root-mean-square error (RMSE) and mean bias (MB) of the predicted half-hourly  $\lambda E$  from the 12 towers were -1.97 and 44.9 W m<sup>-2</sup> with a correlation (r) of 0.90 (Table 3), respectively. The RMSE of individual sites varied between 35.6 and 57.5 W m<sup>-2</sup> with an r of 0.88– 0.96 (Table 3). On the daily scale, the RMSE varied from 13 to 31.1 W m<sup>-2</sup>, with an overall RMSE of 20.9 W m<sup>-2</sup> (Table 3). To determine the ability of the PMBL approach to accurately track the land surface fluxes, a time series comparison between modeled  $\lambda E$ and those from eddy covariance measurements was performed. Two representative sites (one corn and one soybean; Figs. 3a,c) were selected to show the diurnal dynamics of  $\lambda E$  and characterize the response of two different crop types on modeled  $\lambda E$  during the daytime hours from DOY 171 to 189. Figures 3a,c reveal that the temporal  $\lambda E$  dynamics from PMBL over both the corn and soybean were consistent with the observed  $\lambda E$  pattern thorough out the study period. Observed  $\lambda E$  over the corn was about  $80-120 \text{ W m}^{-2}$  greater than the soybeans, and PMBL could clearly detect this difference. Scatterplots of  $\lambda E$  predictions from PMBL against measured  $\lambda E$  at all the corn and soybean tower sites revealed the performance of PMBL to be relatively better over the soybean, as compared to the corn (Figs.

3b,d; Table 3). This, we think, could be because of the relatively uniform vegetation cover of soybean canopy as compared to the larger variability seen for corn canopies. For the soybean sites, an even distribution of points around the 1:1 validation line (Fig. 3d) indicates a good fit of predictions with the measured  $\lambda E$ , with r and RMSE of 0.90 and 44.6 W m<sup>-2</sup> and having slope and offsets of r to the order of 0.96 (±0.01) and 19 (±3.7), respectively. For the corn sites, r and RMSE of 0.92 and 46.2 W m<sup>-2</sup> (Fig. 3b; Table 3) was obtained with a slope and offset of r to the order of 0.86 (±0.01) and 32.3 (±3.1).

Transect-averaged  $\lambda E$  from DOY 166 to 186, observed by the Canadian Twin Otter at 40 m above ground level for the 16 aircraft flights, revealed an RMSE and *r* of 38.5 W m<sup>-2</sup> (14% of the observed mean) and 0.90 (Table 3; Figs. 3e,f). The data of individual flight tracks are pooled together, and the temporal comparison of the PMBL  $\lambda E$  with the aircraft fluxes revealed a coherent behavior (Fig. 3e).

The validation results over GCIP were equally promising, with a correlation between the predicted and measured  $\lambda E$  to be 0.90, 0.94, and 0.91 for the three individual crop years (1997, 1998, and 1999). The RMSE for all the three years was 41.6, 34.6, and 41.6 W m<sup>-2</sup>



FIG. 3. Time series comparison of observed  $\lambda E$  (black line) and PMBL predictions (gray squares) for (a) corn (WC33), (c) soybean (WC03), and (e) aircraft-measured during SMEX-02, along with the pooled validation of  $\lambda E$  for all the (b) corn, (d) soybeans, and (f) aircraft transect flight paths for every individual day during SMEX-02. In (e), the transect data along flight paths of every individual day were averaged to produce the time series. The plot in the inset of (f) is the 1:1 validation of transect-averaged  $\lambda E$  vs PMBL $\lambda E$ . Any gap in the time series is caused either by the absence of flux measurements or missing ancillary data.

(Table 3). An illustrative example of the 1:1 validation plot (Fig. 4a) for the year 1998 revealed a good fit of the  $\lambda E$  predictions, with a slope and offset of 0.95 (±0.004) and 1.93 (±0.52). The temporal comparison (Fig. 4b) of the measured and predicted  $\lambda E$  during the active vegetative phase of soybeans revealed the efficacy of the proposed approach in tracking the pattern of  $\lambda E$  for both the high and low magnitude.

Having retrieved  $\lambda E$ , we also assessed the magnitude of surface energy balance closure  $[(\lambda E + H)/(R_N - G)]$ 

based on the estimated  $\lambda E$  and observed H,  $R_N$ , and G. The magnitude of closure was 75% for SMEX-02 and 78% for the GCIP.

## 2) TROPICAL EDDY COVARIANCE AND FLUXNET

The approach was also applied on monthly data over 21 different tropical rain forest locales. The evergreen rain forest sites spanning over the equatorial band showed the best results (Table 4) with an overall RMSE



FIG. 4. (a) Pooled 1:1 validation of measured vs PMBL $\lambda E$  over the eddy covariance sites of Bondville during GCIP for the year 1998. This produced a correlation of 0.94 with a gain and offset of correlation 0.95 (±0.004) and 1.93 (±0.52), respectively. (b) Comparison of time series of tower measurements (black line) vs PMBL (gray squares)  $\lambda E$  during the active vegetative phase of soybeans in 1998.

of 23.8 W m<sup>-2</sup> and an *r* of 0.92 (Table 4). The RMSE varied between 6.6 and 52.1 W  $m^{-2}$  across the tropical rain forest sites, with r varying from 0.31 to 0.98 (Table 4). Among all the sites, maximum RMSE (52.1 W  $m^{-2}$ ) was obtained for the La Selva (LAS) site. All the Amazon sites (BAN, CAX, M14, M34, KM67, and KM83) in the South America subnetwork showed consistently good results, with the exception of the KM77 site, where RMSE was relatively high (45.9 W  $m^{-2}$ ; see Table 4 for the complete list of sites and their abbreviations). An intercomparison of our  $\lambda E$  with the PT-JPL  $\lambda E$  (Table 4) revealed nearly similar statistics, and the difference in the overall RMSE between the two approaches was only 4.6 W m<sup>-2</sup>. Sitewise comparison revealed the maximum difference in RMSE between the two approaches to be approximately 20 W  $m^{-2}$ .

The  $\lambda E$  estimates from our method over the 15 FLUXNET sites also produced good agreement with the observations and captured nearly 90% variability of the monthly  $\lambda E$ , with an RMSE of 29 W m<sup>-2</sup> or approximately 15 mm month $^{-1}$  (Table 5). RMSE varied between 8.5 and 53.7 W m<sup>-2</sup>. Overall, r between the predicted and measured  $\lambda E$  was 0.89. Here also, an intercomparison of our  $\lambda E$  with the PT-JPL  $\lambda E$  estimates was done and is summarized in Table 5. The maximum difference in RMSE between the two approaches was found in Virginia Park (around 18 W  $m^{-2}$ ). For rest of the FLUXNET sites, the RMSE difference between the two approaches varied from 5 to 10 W m<sup>-2</sup>. However, the mean bias revealed a consistent overestimation of  $\lambda E$  by both PMBL and PT-JPL over a majority of the sites (Table 5).

Illustrative examples of the temporal dynamics of tropical forest  $\lambda E$  over two continents (South America and Southeast Asia) falling under diverse climatic settings are shown in Figs. 5a,b. The example revealed the efficacy of the proposed approach in capturing both

the high-frequency and low-frequency fluctuations in the monthly  $\lambda E$ . Similarly, the temporal pattern of  $\lambda E$ over a broad range of biomes in the FLUXNET eddy covariance network (Figs. 5c,h) also revealed the efficiency of the proposed approach to track the year-round dynamics in  $\lambda E$ .

Given the significance of  $\lambda E$  as an essential climate variable, annual evaporation (E) was also analyzed for both the tropics and FLUXNET sites (Figs. 6a-d). Annual evaporation was computed by summing the monthly values. If, in any year, an observed or estimated E value in a month was missing, that particular year was not included in the computation. Over the tropics, the overall RMSE of annual E from our approach was 103 mm (Table 4), which was 13% of the observed mean, as opposed to 157 mm from the PT-JPL. For the FLUXNET sites, an overall RMSE of 119 mm (Table 5) was obtained with PMBL, which was higher than the RMSE obtained by PT-JPL (110 mm yr<sup>-1</sup>). The overall correlation between the proposed approach and observed annual E was 0.95 over the tropics and 0.86 over the FLUXNET, respectively. An overestimation tendency of annual E over the FLUXNET sites for both PMBL and PT-JPL was evident from Table 5 and Figs. 6c,d.

The South American subnetwork of towers was mostly concentrated in Amazonia. Observed annual Evaried between 548 and 1243 mm across all the Amazon basin stations, and our estimates varied between 536 and 1208 mm (Fig. 6b). In South America, the highest E was found in LAS at about 1243 mm with a very high interannual and month-to-month variability. Over Southeast Asia, the variability of the annual E is quite high among sites, with a range varying from as low as 240 mm [Mae Klong (MKL)] to as high as 1209 mm [Palangkaraya (PKA)] (Fig. 6b). The E outputs from PMBL have also captured a similar pattern,

TABLE 5. Intercomparison of PMBL  $\lambda E$  statistics against  $\lambda E$  observations and PT-JPL  $\lambda E$  model for the individual eddy covariance subnetwork of FLUXNET. Abbreviations: CRO, cropland; GRA, grassland; DBF, deciduous broadleaf forest; ENF, evergreen needleleaf forest; EBF, evergreen broadleaf forest; WET, wetland; and SAV, savanna.

					)	$E_{\rm PMBL}$		λ	$E_{\rm PT-JPL}$	
FLUXNET	Site	Biome	Latitude (°)	Longitude (°)	RMSE (W m <sup>-2</sup> )	$\frac{MB}{(W m^{-2})}$	r	RMSE (W m <sup>-2</sup> )	$\frac{MB}{(W m^{-2})}$	r
AmeriFlux	Bondville (BOND)	CRO	40.006	-88.290	21.6	5.6	0.97	23.6	5.4	0.96
	Howland (HOW)	ENF	45.204	-68.740	38.8	29.0	0.89	26.3	-4.9	0.94
	Mize (MIZ)	ENF	29.764	-82.245	33.0	2.7	0.83	25.5	2.7	0.93
	Morgan Monroe (MMS)	DBF	39.323	-86.413	34.9	22.9	0.97	32.3	29.0	0.98
	Niwot Ridge (NR)	ENF	40.033	-105.546	26.7	20.5	0.93	15.3	-3.0	0.95
	Tonzi Ranch (TON)	SAV	38.432	-120.966	30.4	11.1	0.79	25.4	14.3	0.87
	Walnut River (WAL)	GRA	37.521	-96.855	25.8	3.6	0.94	9.4	-3.7	0.99
EuroFlux	Griffin (GRIF)	ENF	56.607	-3.798	11.7	-5.8	0.97	12.7	-2.7	0.96
	Hainich (HAI)	DBF	51.079	10.452	17.9	12.6	0.95	23.4	17.0	0.96
	Hesse (HES)	DBF	48.674	7.064	18.7	11.8	0.97	22.8	18.0	0.98
Fluxnet	Mer Bleue (MER)	WET	45.409	-75.519	8.5	1.3	0.99	17.2	2.3	0.98
Canada	Northern Study Area–Old Black Spruce (OBS)	ENF	53.987	-105.118	19.9	15.0	0.91	11.5	-2.1	0.91
OzFlux	Tumbarumba (TUM)	EBF	-35.656	148.152	33.7	25.0	0.92	23.5	0.7	0.91
	Virginia Park (VIR)	SAV	-19.883	146.553	53.7	47.6	0.60	37.0	34.3	0.89
AsiaFlux	Takayama (TAK)	DBF	36.146	137.423	21.9	17.7	0.92	33.4	29.0	0.88
Pooled	_	_	_	_	29	13.1	0.89	23.6	9.5	0.95
Annual (mm)	—	—	—	—	119	83	0.86	101	53	0.86

thus revealing its potential to capture the wide variability of annual E in Southeast Asia. Among the five subnetworks of FLUXNET, the maximum among site variability in annual E (371–823 mm) was found in AmeriFlux and the minimum variability (341–448 mm) was found within the EuroFlux. This pattern was also captured by our approach (Fig. 6d); however, its performance was relatively weaker for the five sites (HOW, NR, MMS, TUM, and VIR; see Table 5 for full site names) where annual E was significantly overestimated (Fig. 6d).

Observational evidence of the decline in the annual Eover the central Amazon was noted for the year 2005, and our approach also captures this well. For example, there was a sharp decrease of 33% in the annual E from 630 to 420 mm in the Manaus KM34 (M34) between 2000 and 2006 (Fig. 7a). The annual E over Ecotonal Bannanal plantation reduced about 17% from 2004 to 2005 (Fig. 7b). M34 has often been treated as a benchmark reference site for land atmosphere interaction studies over the Amazon (Pielke et al. 2011), and this sharp decline in the annual E supports the extended drought period in the Amazon that was initiated by an El Niño in 2002/2003, followed by warming of the tropical Atlantic sea surface in 2004/2005. The decline in rainfall for the 2004/2005 drought was moderate, but because it followed on the heels of an El Niño, the rainforest had a limited wet spell in between the two dry periods and could not recharge.

### b. Analysis of canopy conductance $(g_S)$

### 1) $g_S$ versus VPD and $\lambda E$

### (i) SMEX-02–SMACEX and GCIP

Since no observation of  $g_S$  was available, its validation could not be possible. Analysis of  $g_S$  was carried out in relation to the observed global radiation  $(R_G)$  [or photo synthetically active radiation (PAR)], VPD, and  $\lambda E$ (Niyogi and Raman 1997). The magnitude of  $g_S$  during SMEX-02 varied between 0.001 and 0.05 m s<sup>-1</sup> for both of the crops, and no significant difference in  $g_S$  was obtained between the two crops, with a mean  $g_S$  of around 0.015 m s<sup>-1</sup>. Clearly,  $g_s$  was 0 m s<sup>-1</sup> at night in the absence of net available energy. A plot of  $g_S$  with VPD (Figs. 8a,b) revealed that  $g_S$  reached a maximum level under low VPD and decreased with increasing VPD. For both corn and soybeans,  $g_S$  showed a sharp exponential decrease (negatively logarithmic) with an increase in the VPD pattern, depending upon varying degrees of  $R_G$ . Figure 8a shows the responses of  $g_S$  to VPD separated by five different levels of  $R_G$  groups. Five negatively logarithmic scatters fit the data with r values of 0.62 (0 < $R_G < 150 \text{ W m}^{-2}$ ), 0.84 (150 <  $R_G < 300 \text{ W m}^{-2}$ ), 0.88  $(300 < R_G < 450 \text{ W m}^{-2}), 0.86 (450 < R_G < 600 \text{ W m}^{-2}),$ and 0.85 ( $R_G > 600 \text{ W m}^{-2}$ ). For soybeans, the *r* values of the exponential scatter (Fig. 8b) for the similar five levels of  $R_G$  were 0.64, 0.85, 0.89, 0.85, and 0.82. For both the crops, the sensitivity of  $g_S$  to VPD was at a maximum in the  $R_G$  range of 300–450 W m<sup>-2</sup> and the sensitivity of



FIG. 5. (b) Comparison of time series of tower measurements vs PMBL and PT-JPL  $\lambda E$  for the representative sites of the (a) South American (Santarem KM67), and (b) Southeast Asian (Mae Klong) subnetworks; (c)–(h) similar comparison over representative sites covering six broad spectrums of biome types of the FLUXNET eddy covariance network.

 $g_S$  to VPD decreased when  $R_G$  was lesser than 150 W m<sup>-2</sup> (Niyogi et al. 1998).

Two dimensional scatters between  $g_s$  and observed  $\lambda E$  (Figs. 8c,d) revealed linearity when plotted for different levels of VPD. This shows that  $g_s$  tends to decrease with increasing VPD without any increase in the  $\lambda E$ , like an inverse hyperbolic pattern to VPD (Monteith 1995). Stomatal regulation tended to keep the  $\lambda E$  constant when the VPD was changed from low (10–15 hPa) to high magnitude (>25 hPa) (Figs. 8c,d).

This also revealed the sensitivity of  $g_S$  to  $\lambda E$  to be directly proportional to VPD. The correlation of the scatter between  $g_S$  and  $\lambda E$  for the varying levels of VPD was highest (r = 0.91 for corn and r = 0.89 for soybeans) at 20 > VPD > 10 hPa. The least correlation (0.40 for corn and 0.35 for soybeans) was found at VPD < 5 (Figs. 8c,d).

Illustrative examples of the diurnal pattern of  $g_S$  for both corn and soybeans (Figs. 8e,f) revealed that  $g_S$ closely follows the shortwave radiation ( $R_G$ ) pattern, and peak  $g_S$  was found before the noon (between 1000



FIG. 6. (a) Validation of individual year-wise annual E over the tropics using PMBL. PMBL produced an overall r of 0.95 ( $R^2 = 0.90$ ), with a slope and offset of r (black solid line) to be 0.83 (±0.03) and 136.15 (±28.69), respectively. (b) Histogram comparison of mean annual E between PMBL and PT-JPL by averaging all the individual year E values over 21 tropical eddy covariance sites. The number of years in this averaging varied from at least three to a maximum of seven. (c),(d) As in (a),(b), but over only the FLUXNET sites; PMBL produced an overall r of 0.87, with a slope and offset of r (black solid line) to be 0.89 (±0.09) and 135.05 (±45.58), respectively. The histograms are from 15 FLUXNET sites. The number of years in this averaging varied from at least two to a maximum of five.

and 1100 LT) when the water use efficiency was high because of ample  $R_G$  and low saturation deficits. Thereafter,  $g_S$  decreased steadily for the rest of the day as VPD increased, and  $R_G$  levels fell in the afternoon. Because of multiple controls on  $g_S$ , particularly the strong control of  $R_G$  at midday, the diurnal patterns of  $g_S$  did not show a negative correlation with VPD until it followed a certain level of  $R_G$  during the course of a day (Figs. 8e,f). Once it attained its peak,  $g_S$  started falling in the afternoon, even with the increase in  $R_G$  and VPD (Niyogi et al. 2009).

For the GCIP also,  $g_S$  was strongly reduced with an increase in VPD; about a 50% reduction was noted when VPD increased from 10 to 20 hPa. The negative logarithmic relationship between  $g_S$  and VPD was found by grouping  $g_S$  on the basis of  $R_G$  on the half-hour temporal data. Five negatively logarithmic scatters (Fig. 9a) fit the data with r values of 0.58 (0 <  $R_G$  <

150 W m<sup>-2</sup>), 0.61 (150 <  $R_G$  < 300 W m<sup>-2</sup>), 0.66 (300 <  $R_G$  < 450 W m<sup>-2</sup>), 0.66 (450 <  $R_G$  < 600 W m<sup>-2</sup>), and 0.69 ( $R_G$  > 600 W m<sup>-2</sup>). The correlation coefficients of the exponential scatters are again indicative of the high sensitivity of  $g_S$  to VPD for the magnitude of  $R_G$  at or above 150 W m<sup>-2</sup>. Here also, the correlation of the scatter between  $g_S$  and  $\lambda E$  for the varying levels of VPD was highest (r = 0.81) at 10 < VPD < 15 hPa, and the relationship strength was lowest at VPD < 5 hPa (Fig. 9b).

Diurnal behavior of  $g_S$  with  $R_G$  and VPD during GCIP was very similar to that observed over SMEX-02. An example of diurnal dynamics for five consecutive days during the active growth stage of soybeans clearly revealed a midday depression in  $g_S$ , which may be caused by peak VPD at midday (Fig. 9c). For relatively good moisture availability,  $g_S$  responds directly to rising  $R_G$  in the morning hours; in the later part of the day, it inversely



FIG. 7. Time series of annual E over two representative sites: (a) Manaus KM34 (central Amazon) and (b) Bannanal Island (BAN) (southern Amazon) of the Amazonian rain forest. This clearly shows a significant decrease in the E during 2004/2005, and PMBL is capable of capturing this declining trend in E for 2004–05 along with PT-JPL.

responds to increasing VPD, and again, in the very late afternoon, it responds directly with decreasing  $R_G$ . Thus, the maximum value of  $g_S$  is mostly found in the morning (Niyogi et al. 2009).

### (ii) Tropical forest and FLUXNET

The magnitude of monthly  $g_S$  over the tropics varied from 0.005 to 0.035 m s<sup>-1</sup>. As in previous experiments, here also the scatters between  $g_S$  and VPD revealed an exponential decline of  $g_S$  with rising VPD (Fig. 10a). Three exponential scatters fit the data with *r* values of 0.51 (0 <  $R_N$  < 150 W m<sup>-2</sup>), 0.54 (150 <  $R_N$  < 300 W m<sup>-2</sup>), and 0.66 (300 <  $R_N$  < 450 W m<sup>-2</sup>). Linear response of  $g_S$  with  $\lambda E$  (Fig. 10b) for different thresholds of VPD was also found. A 50% reduction in the  $g_S$  was found with a rise in VPD from 10 to 20 hPa at a constant level of  $\lambda E$ .

The nature of scatter and correlation between  $g_S$  versus VPD and  $g_S$  versus  $\lambda E$  was similar over the FLUXNET (Figs. 10c,d). The correlation of the exponential scatter between  $g_S$  and VPD was maximum (0.66) for  $300 < R_N < 450$  W m<sup>-2</sup> and least (0.51) for  $R_N < 150$  W m<sup>-2</sup>. Similarly, the correlation of the linear scatter between  $g_S$  and  $\lambda E$  was maximum (0.98) for VPD > 25 hPa and least (0.64) for VPD < 5 hPa.

### 2) $g_S$ VERSUS GROSS PRIMARY PRODUCTION

Given  $g_S$  is the "coupler" between  $\lambda E$  and photosynthesis [net primary productivity (NPP)], the dependence

of  $g_S$  on gross primary production (GPP) is also analyzed (NPP data were not available). Figures 11a,b show the response of GPP to  $g_s$ . After an initial increase, the response of GPP became asymptotic and the carbon gain slightly declined after a  $g_s$  of 0.02 m s<sup>-1</sup>. Plants use their stored carbon conservatively; they are much more efficient in controlling  $g_S$  when atmospheric VPD is low and surface moisture is high in the morning hours, so that the stored carbon can be utilized later to moderate the impacts of high afternoon VPD (Niyogi and Xue 2006). Substantial diurnal hysteresis was found in the plot of  $g_S$  against GPP, VPD, and  $R_G$  (Fig. 11c).  $R_G$  represents the driving force for GPP, but VPD controls the  $g_S$  through imposing limitation on stomatal opening. Although  $R_G$  and VPD tend to covary throughout a day, their variation is out of phase on clear days. As a result, the variation of  $g_s$  is also out of phase with GPP.

### c. Sensitivity analysis

Relative sensitivity of the derived  $\lambda E$  to perturbations in four critical radiation and meteorological variables (Table 6) revealed  $\lambda E$  to be the most sensitive to the uncertainties in the  $R_N$ , and an error in  $R_N$  of  $\pm 10\%$  can produce a relative error of 22%–24% in the  $\lambda E$  estimates (Niyogi et al. 1999). Among other variables, the relative humidity proved to be the second-most sensitive variable at a lower range (60%-70%), where a 10% uncertainty may produce an error of 12%. The sensitivity of  $\lambda E$  to  $T_a$  and G was very small, 4%–8% and 4%-6%, respectively. Given the measurement accuracy of the current generation  $R_N$  (±10%),  $T_a$  (±2%), and RH (±1%) measurement sensors, the potential uncertainty of our estimates of  $\lambda E$  may be 20%–25% if the sensor uncertainty is additive. However, the errors tend to cancel each other out if the uncertainties of the input variables are in the opposite direction. Uncertainty may be reduced when applied from the remote sensing platform because the accuracies of  $R_N$ ,  $T_a$ , and RH from current generation satellites are 5 W m<sup>-2</sup> (http://ceres. larc.nasa.gov/science\_information.php),  $\pm 1$ K, and  $\pm 10\%$ (Tobin et al. 2006), respectively. The current uncertainty analysis does not explicitly address sensitivity of PMBL to multiple variables. Multivariate sensitivity may either enhance the cumulative error or may cancel out each other's effects and thus may reduce the overall errors.

### 6. Discussion

For the experimental and tower network data, the residual error (predicted – observed) in the  $\lambda E$  was influenced by M (RH<sup>VPD</sup>) and VPD (Figs. 12a,d);  $T_a$  and  $\Phi$  do not have much influence on the residual error



FIG. 8. Response of  $g_S$  to changes in the VPD for (a) corn and (b) soybeans during SMEX-02. The behavior of retrieved  $g_S$  with observed  $\lambda E$  for different classes of VPD in (c) corn and (d) soybeans. (e) Illustrative examples of the diurnal patterns of  $g_S$  (blue line),  $R_G$  (W m<sup>-2</sup>) (red line), and VPD (hPa) (green line) over five consecutive days for corn and (f) soybeans, respectively, during SMEX-02.

(Figs. 12b,c). This was evident for all of the sites where the residual error was negative (predicted < observed) up to M values of 0.25, and it was consistently positive beyond M values of 0.25 (Fig. 12a) up to M = 0.75. For the intermediate ranges of VPD (10–20 hPa), the residual error was consistently positive, whereas for VPD >20 hPa, the error was in both direction. The formulation of M is based on the hypothesis that equilibrium exists between atmospheric and surface moisture and under the condition of extreme surface dryness and high evaporative demand (VPD); no water vapor can be transferred into the atmosphere because of unavailability of water in the surface. The vapor pressure deficit was treated as a proxy to bridge between surface dryness and high evaporative demand, but such equilibrium assumption may be violated and VPD may not truly capture the entire dryness or wetness regime from the surface to subsurface. Plants can extract some moisture through roots to transpire if some moisture is present in the root zone. Under such conditions the RH<sup>VPD</sup> expression may underestimate the wetness, and resultant  $\lambda E$  will also be underestimated. This might be the reason for consistent underestimation of  $\lambda E$  and higher RMSE in corn compared to soybeans, as reported in section 5a(1) and Table 3. Also, corn has spatially variable leaf area index (LAI) as compared to soybean. As a result the values of  $\lambda E$  on corn have higher variability and also result in possible poor predictions as



FIG. 9. (a) Response of stomatal conductance ( $g_S$ ) in relation to VPD for different levels of  $R_G$  over the eddy covariance sites of Bondville during GCIP. (b) Dependence of  $\lambda E$  on  $g_S$  for different levels of evaporative demand (VPD) over Bondville during GCIP. This example is shown pooling all the 30 min data for the year 1998. (c) Diurnal patterns of  $g_S$  (blue line),  $R_G$  (W m<sup>-2</sup>) (red line), and VPD (hPa) (green line) over five consecutive days over Bondville during GCIP.

compared to the soybeans. Corn has a longer root length that is capable of extracting water from deeper layers. PMBL does not include any crop ecophysiological characteristics to capture these behaviors. On the contrary, for the intermediate dryness-wetness condition, *M* might have been overestimated, resulting in overestimation of  $\lambda E$ . The overestimation of  $\lambda E$ through PMBL in the FLUXNET mainly stemmed from the Howland, Niwot Ridge, Morgan Monroe, Tonzi Ranch (Fig. 6d), Tumbarumba (Fig. 6g), and Virginia Park sites (Table 5). This may again be because of violation of assumption of equilibrium between M and the relative soil moisture in these sites, particularly during the dry-down phase. This also points to the importance and necessity of including the radiometric surface temperature in the terrestrial evapotranspiration modeling to capture the surface moisture controls on  $\lambda E$ .

The intersite variability of  $\lambda E$  over all the SMEX-02 corn sites was quite consistent between measurements (Su et al. 2005; Prueger et al. 2005), but disparities

between measurements for soybeans (e.g., in WC13) were also reported between site locations (Su et al. 2005; Prueger et al. 2005). This might also have affected the overall accuracy of the proposed approach. There are reports of systematic overestimation of  $R_N$  (20%; Kustas et al. 1998) and underestimation of  $\lambda E$  (20%– 25%; Wilson et al. 2002) in the eddy covariance measurements. Even if there is no error in  $R_N$  and  $\lambda E$ measurements, the  $\lambda E$  evaluation between the PMBL and tower would change by a small amount, leading to little or no net change in the overall evaluation for  $\lambda E$  (since we have closed the surface energy balance). However, for better accuracy of such a modeling approach, the forcing state variables need to be more quality controlled. This is even more crucial at high-frequency temporal scales, where the probabilities of losing fluxes are at a maximum (Foken et al. 2004; Massman and Lee 2002; Moncrieff et al. 1997). One of the reasons for the relatively better accuracy of PMBL over the tropics and FLUXNET is because many random noises get filtered out in the monthly averaging.



FIG. 10. Dependence of  $g_s$  in relation to (a) VPD for different levels of  $R_N$  over the tropics, (b)  $\lambda E$  for different levels of evaporative demand (VPD) over the tropics, (c) VPD for different levels of  $R_N$  over FLUXNET, and (d)  $\lambda E$  for different levels of evaporative demand (VPD) over FLUXNET.

From the tropical sites and the periods of analysis, it is evident that  $R_N$  is the prime driver of  $\lambda E$  over the equatorial rain forests, and  $\lambda E$  utilized approximately 65%–70% of  $R_N$ . This finding is consistent with the findings from field observations throughout the Amazonian rain forest (Malhi et al. 2002; Fisher et al. 2009). Among the two poorly validated tropical sites [LAS and Santarem KM77 (KM77)], KM77 experienced severe anthropogenic disturbances due to the biomass burning during this period (Fisher et al. 2009). This might have reduced the observed  $\lambda E$  magnitude. Since no impact was found in the driving variables ( $R_N$ , G,  $T_a$ , and RH), PMBL was unable to track down these sudden falls in  $\lambda E$  and produce significantly high RMSE. Clearly, in a majority of the cases, a close correspondence in  $\lambda E$  estimates was found from both PMBL and PT-JPL, but they differ in some cases. Despite sharing the common moisture scalar equation  $(M = RH^{VPD})$  with PT-JPL, PMBL uses only radiation and meteorological variables for estimating  $\lambda E$ , while PT-JPL uses reflectance information to parameterize plant moisture constraint and other scalars. Such differences might have led to the disagreement between the two approaches in the La Selva site.

Sensitivity analysis clearly shows  $R_N$  to be the most important variable. All the observations in the present analysis used an all-wave net radiometer, which has typical uncertainties of  $\pm 10\%$ . However, use of four component net radiometers might help reduce some errors in future studies.

The scatters between  $g_S$  versus  $\lambda E$  and  $g_S$  versus VPD from all the datasets (Figs. 8-10) provided convincing evidence about the environmental response of stomata. The estimates of  $g_S$  are dependent on VPD; however, we have not specified  $g_S$  to behave exponentially with VPD. Still,  $g_S$  revealed the exponential behavior when linked with VPD, which is a classic pattern. This highlights the fidelity of the analytical approach. Linking  $g_S$  with independently measured  $\lambda E$  revealed a distinct linearity between the two, and the slope of the linearity varies with the VPD. This is another theoretical finding of Monteith and indicates that our retrieval is consistent. An earlier hypothesis of Monteith (1995) showed that  $g_s$ decreases linearly with  $\lambda E$  when VPD changes (with an inverse hyperbolic relation). The change in  $g_S$  is dominated by an increase in net energy input, but this change is partially offset by an increase in  $\lambda E$  rate. After the net



FIG. 11. Dependence of  $g_S$  on GPP for (a) corn and (b) soybeans during SMEX-02. (c) Illustrative example of the diurnal course of  $g_S$  (blue line) with GPP (black line, mg m<sup>-2</sup> s<sup>-1</sup>),  $R_G$  (W m<sup>-2</sup>, red line), and VPD (hPa, green line).

energy input in the system exceeds a certain threshold,  $g_S$  starts decreasing even if  $\lambda E$  increases. This supports the hypothesis that the stomata responds to VPD through a "feedback" mechanism based on the effect of  $\lambda E$  on water potential gradient between the guard cells (Monteith 1995; Jones 1998). This is also the reason  $g_S$  typically peaks before noon and there is partial shutdown of stomata during the afternoon (Kramer and Boyer 1995).

The control of soil moisture to transpiration also became evident from the scatter between  $g_S$  and  $\lambda E$  for different VPD levels. This supports the findings of Denmead and Shaw (1962), who hypothesized reduced stomatal conductance and stomatal closure at higher levels of soil moisture (high  $\lambda E$  as well) when the atmospheric demand of water vapor increases (high VPD). This is apparent because the moisture content in the immediate vicinity of the root depletes rapidly at high atmospheric demand. This decreases the soil conductivity, and the soil will not be able to supply water immediately.

The observed scatter between GPP and  $g_s$  supports the fact that, when the soil moisture is available, their relationship is approximately linear (Tuzet et al. 2003; Meinzer et al. 1997). This was evident from data points over the corn and soybeans during SMEX-02. However, there may be hysteresis in the relationship under limiting surface moisture conditions (Tuzet et al. 2003), as found in the scatter and from the temporal behavior of  $g_S$  and GPP (Fig. 11). Such kinds of scatters are common when all the environmental variables that control  $g_S$  covary under the variable dry–wet cycle and the spread in the scatter increases as the surface dries out.

The prediction accuracy of hourly and monthly  $\lambda E$  from the proposed approach is comparable with the results reported using the similar datasets and over other

TABLE 6. Sensitivity of PMBL-derived  $\lambda E$  to different core variable inputs.

Variables	Sample range	Error	Sensitivity
$T_{a}$	15°–20°C	±2°C	0.08
-	20°–25°C	±2°C	0.06
	25°-30°C	±2°C	0.04
RH	60%-70%	$\pm 10\%$	0.12
	70%-80%	$\pm 10\%$	0.09
	80%-90%	$\pm 10\%$	0.07
$R_N$	400-500 W m <sup>-2</sup>	$\pm 10\%$	0.22
	500-600 W m <sup>-2</sup>	$\pm 10\%$	0.23
	$600-700 \text{ W m}^{-2}$	$\pm 10\%$	0.24
G	100-110 W m <sup>-2</sup>	$\pm 10\%$	-0.04
	110-120 W m <sup>-2</sup>	$\pm 10\%$	-0.05
	120-130 W m <sup>-2</sup>	±10%	-0.06



FIG. 12. Mean and standard deviation ( $\sigma$ ) of the residual error in PMBL  $\lambda E$  for various ranges of (a)–(d) M (RH<sup>VPD</sup>),  $T_a$ ,  $\Phi$ , and VPD, respectively.

data in various regional and global studies based on the Priestley–Taylor and Penman–Monteith approaches. Over the agroecosystems, our results are also comparable with the one-source and two-source residual energy balance models. While estimating  $\lambda E$  during the SMEX-02–SMACEX experiment, Su et al. (2005) obtained an RMSE of 47 W m<sup>-2</sup> over corn and 40– 48 W m<sup>-2</sup> over soybeans using a single source  $\lambda E$ model. Series of experimental results have been published based on the two source  $\lambda E$  models (Mecikalski et al. 1999; Anderson et al. 2007, 2008), where the RMSE range varied between 37 and 66 W m<sup>-2</sup> for hourly  $\lambda E$ .

#### 7. Summary and conclusions

We conclude that the combination of net available energy, air temperature, and vapor pressure deficit in the framework of Penman–Monteith, Priestley–Taylor, and Bouchet's complementary hypothesis showed significant promise for estimating  $\lambda E$  when compared with independent observations of eddy covariance tower ground truth data. It provides a relatively better estimate than the Priestley–Taylor–based model over the tropics and a majority of the FLUXNET sites. The strength of this approach may be manifold: 1) it may be helpful to assess and test the land surface parameterization embedded in climate–Earth system models, and 2) in the developing countries of Southeast Asia and Africa, this method may offer a cost effective way for generating  $\lambda E$  information from a network of automatic weather stations. The results also warrant further investigation, particularly into refinements in the representation of the surface wetness (or moisture). The results point to the use of radiometric surface temperature, which is a direct physical quantity in these regards and also a direct indicator of surface-to-root zone wetness (Norman et al. 1995; Kustas et al. 2005; Anderson et al. 2007). Where the method appears to work, this provides estimates of  $\lambda E$  that would prove valuable in a range of applications. The ability to accurately predict stomatal conductance as a function of environmental variables would be useful in spatially explicit hydrology and climate modeling and predicting vegetation responses to global change.

The advent of Earth observation sciences may afford an opportunity to extend the PMBL methodology into the satellite platform by integrating the satellite  $R_N$ from Clouds and the Earth's Radiant Energy System (CERES) or Surface Radiation Budget (SRG),  $T_a$  and  $R_H$  from the Atmospheric Infrared Sounder (AIRS), and soil moisture from the Soil Moisture and Ocean Salinity Mission (SMOS) and the future Soil Moisture Active Passive (SMAP), thus allowing for more spatially explicit hydrological and physiological process studies.

Acknowledgments. We gratefully acknowledge NSIDC and CEOP for making the SMEX-02 and GCIP data available. K.M. acknowledges the comments from Dr. Bill Kustas, HRSL, USDA, and Dr. B. K. Bhattacharya, Space Applications Centre, India. We also acknowledge the site PIs of the tropical forest eddy covariance network and FLUXNET network for the data permission. We acknowledge Dr. John Prueger for permitting us to use the SMEX-02. K.M. also acknowledges Dr. Junhak Lee for his help in map preparation and the postdoctoral research fellowship from the Jet Propulsion Laboratory's Research and Technology Development Climate Strategic Initiative. D.N. benefited in part through NSF CAREER (AGS-0847472, Anjuli Bamzai), USDA NIFA 2011-68002-30220, and NSF INTEROP OCI 0753116. KM was partly funded by the Natural Environment Research Council, United Kingdom, Grant NEE0191531. Three anonymous reviewers are also acknowledged for their helpful comments. The research was carried out at the Jet Propulsion Laboratory, California Institute of Technology, under a contract with the National Aeronautics and Space Administration.

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